RGB Color Code - selected colors expressed in hexadecimal \& decimal values

| - Red | 255:0:0 | FF0000 |
| :--- | :--- | :--- |
| - Green | 0:255:0 | 00FF00 |
| - Blue | 0:0:255 | 0000FF |
| - White | 255:255:255 | FFFFFF |
| - Black | 0:0:0 | 000000 |

- describe the essential characteristic of all shades of gray
$n: n: n$ for $((n>=0) \&(n<=255))$
or
xxxxxx for (( $x>=0) \&(x<=F))$

The RGB for one shade of sea green is 99CC66 or 153:204:102.
The RGB for one shade of sea blue is 6699FF or 102:153:255.
What is the color specification that describes the color which is produced by changing the sea green color toward the sea blue color by

- reducing the red component of the sea green color by $50 \%$ of the difference between the two colors
- reducing the green component of the sea green color by $25 \%$ of the difference between the two colors
- increasing the blue component of the sea green color by $25 \%$ of the difference between the two colors

| 153 | 204 | 102 |
| :--- | :--- | :--- |
| $\frac{102}{51}$ | $\frac{153}{51}$ | $\frac{255}{-153}$ |
| $\Delta \downarrow 50 \%$ | $\Delta \downarrow 25 \%$ | $\Delta \uparrow 25 \%$ |
| $51 / 2 \approx 25$ | $51 / 4 \approx 13$ | $-153 / 4 \approx-38$ |
| 153 | 204 | 102 |
| $\frac{-25}{128}$ | $\frac{-13}{191}$ | $\frac{+38}{140}$ |

Answer: 128:188:140

Describe how analog sound waves are converted to digital representation. What role does the Nyquist Rule play in the conversion process?

The analog sound wave must be sampled at regular intervals, i.e., the amplitude is measured at each interval and the two numbers are stored in digital form, i.e., sequences of bi-tuples <time interval, amplitude>.


Amplitude is a measure of the "Sound Pressure".
The Nyquist Rule states that the Sampling Rate must be at least twice as fast as the fastest frequency being recorded. That means that the distances between the intervals must be $1 / 2$ of the shortest wave length being recorded.
Since
wavelength $=\frac{1}{\text { frequency }}$
then the Nyquist Rule can be restated as follows: the sampling intervals must be at least $1 / 2$ of the shortest wavelength.

Since human perception of sound is limited to approximately $\mathbf{2 0 , 0 0 0} \mathbf{~ H z ~ o r ~} 20$ GHz , the standardized digital audio recording frequency of $44,100 \mathrm{~Hz}$ captures most of the sound which can be heard by the normal human ear.

## Number Systems

| Decimal | Octal | Binary | Hexadecimal |
| :---: | :---: | :---: | :---: |
| 0 | 0 | 0000 | 0 |
| 1 | 1 | 0001 | 1 |
| 2 | 2 | 0010 | 2 |
| 3 | 3 | 0011 | 3 |
| 4 | 4 | 0100 | 4 |
| 5 | 5 | 0101 | 5 |
| 6 | 6 | 0110 | 6 |
| 7 | 7 | 0111 | 7 |
| 8 | 10 | 1000 | 8 |
| 9 | 11 | 1001 | 9 |
| 10 | 12 | 1010 | A |
| 11 | 13 | 1011 | B |
| 12 | 14 | 1100 | C |
| 13 | 15 | 1101 | D |
| 14 | 16 | 1110 | E |
| 15 | 17 | 1111 | F |

## Conversions

Octal $\leftrightarrow$ Binary $\leftrightarrow$ Hexadecimal


Conversions
Decimal $\rightarrow$ Base $n$
Successive Divisions of the Decimal Number by n, preserving the remainders
$65_{10} \rightarrow X_{5}$


$$
65_{10} \rightarrow 230_{5}
$$

## Base $\mathbf{n} \rightarrow$ Decimal

Polynomial Expansion


## Addition

Base $\mathbf{n} \boldsymbol{\rightarrow}$ (1) dump the bucket when it has n stones in it;
(2) add one stone to the bucket on the left


## Subtraction

"Take Away"
When bucket is empty for Base $\mathbf{n} \boldsymbol{\rightarrow}$
(1) remove one stone from the bucket on the left
(2) place $\mathbf{n}$ stones in the bucket that was empty


